

# A kinetic study of the reduction of NO<sub>x</sub> stored on Pt-Ba/Al<sub>2</sub>O<sub>3</sub> catalyst

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## ABSTRACT

A kinetic study for the reduction of NO<sub>x</sub> stored onto a Pt-Ba/Al<sub>2</sub>O<sub>3</sub> LNT catalyst is developed, based on previous experimental work where regeneration of stored NO<sub>x</sub> was accomplished under isothermal wet conditions using ammonia and hydrogen as reducing agents [L. Lietti, I. Nova, P. Forzatti, J. Catal. 257 (2008) 270–282]. The kinetic model developed in the present paper differs from those available in the literature because it considers the most relevant physico-chemical features of regeneration of LNT catalysts under nearly isothermal conditions. It is based exclusively on a consecutive reaction scheme with ammonia as intermediate, as proposed in the previous study, and on a mechanism which considers only surface reactions of stored NO<sub>x</sub>. The model includes the elementary-like steps of adsorption–desorption of hydrogen, ammonia and water at Pt sites, and the lumped steps of reduction of stored nitrates by hydrogen to give ammonia and of reduction of residual stored nitrates by ammonia to give nitrogen. A surface dependent energy of activation for the reduction of nitrates with ammonia is required to describe the data in the T interval 150–300 °C. This is due to the presence of nitrates with high and low reactivity that are envisaged as close and far from the noble metal crystallites, respectively. A low energy of activation (22.94 kJ/mol) is estimated for the reduction of nitrates by hydrogen to give ammonia. This applies above a consumption of  $1.5\text{--}2 \times 10^{-4}$  mol of stored NO<sub>x</sub>/g<sub>cat</sub>, where the residual NO<sub>x</sub> species are expectedly stored far from the Pt crystallites and the rate of their consumption is limited by surface diffusion. Before this consumption level the reaction is limited by the concentration of hydrogen at any temperature in the T interval 150–350 °C. The model is shown to capture the major features of the isothermal experiments performed under wet conditions over Pt-BaO/Al<sub>2</sub>O<sub>3</sub> LNT catalyst with hydrogen and ammonia as reducing agents in the T interval 150–350 °C and is able to describe nicely on a purely predictive basis independent NH<sub>3</sub>-TPSR experiments. However the model underestimates H<sub>2</sub> consumption and net NH<sub>3</sub> production during independent H<sub>2</sub>-TPSR experiments below 100 °C, where the consumption of stored NO<sub>x</sub> is less than  $1 \times 10^{-4}$  mol/g<sub>cat</sub> and is associated with fast regeneration of Ba sites in close proximity to the Pt crystallites. The model is also used to simulate the axial concentration profiles in the reactor for gas and surface species as function of time during regeneration with ammonia.

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## 1. Introduction

NO<sub>x</sub> storage-reduction (NSR) is a promising technology for meeting upcoming stringent regulations on NO<sub>x</sub> emission in particular from light duty diesel engines and lean burn gasoline engines [2,3]. The operation of NSR catalysts (also quoted as Lean NO<sub>x</sub> Trap, LNT) comprises a long lean period in which the NO<sub>x</sub> emitted in the exhaust gases are adsorbed on the catalyst surface in the form of nitrites and nitrates and a short fuel-rich period in which the stored NO<sub>x</sub> are reduced by H<sub>2</sub>, CO and unburned hydrocarbons to give N<sub>2</sub>. The LNT catalysts typically consist of a NO<sub>x</sub> storage component such as Ba or K, and of a noble metal such as Pt that catalyses the oxidation of NO and the combustion of CO and unburned hydrocarbons

during the lean period and the reduction of stored NO<sub>x</sub> during the rich period; these catalysts components are dispersed on high surface area alumina support. The commercial LNT catalysts can also contain other components such as Ce for oxygen storage capacity (OSC) and other noble metals (e.g. Rh) to catalyse the WGSR and the reforming of hydrocarbons.

Ammonia formation and reaction over NSR catalysts during regeneration has been observed and studied [1,4–18]. Castoldi et al. [6] and Nova et al. [9] report catalyst effluent NH<sub>3</sub> slip at the end of regeneration of stored NO<sub>x</sub> by hydrogen over a Pt-Ba/Al<sub>2</sub>O<sub>3</sub> sample; they speculated that regeneration of nitrates in close proximity to Pt (fast NO<sub>x</sub> storage/reduction sites) might account for the production of nitrogen while nitrates less proximal to Pt (slow NO<sub>x</sub> storage/reduction sites) are regenerated later to give ammonia. The importance of coupling between the precious metal and BaO where storage of NO<sub>x</sub> takes place was first addressed by Mazhoul et al. [19]. Pihl et al. [8] found that ammonia formation is favoured at

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## Nomenclature

<i>a</i>	unit cell dimension of the FCC structure
<i>b</i>	vector of the adaptive parameters of the kinetic model
<i>C</i>	concentration of gaseous species (mol/m <sup>3</sup> )
<i>D<sub>Pt cryst</sub></i>	diameter of the Pt crystallite
<i>E</i>	activation energy
<i>E<sub>MIN</sub></i>	minimum value of the energy of activation <i>E<sub>S5</sub></i>
<i>E<sub>MAX</sub></i>	maximum value of the energy of activation <i>E<sub>S5</sub></i>
<i>k<sup>0</sup></i>	pre-exponential kinetic constant
<i>L</i>	reactor length
<i>M</i>	molecular weight
<i>N<sub>Av</sub></i>	Avogadro number
<i>N<sub>NO<sub>x</sub></sub></i>	number of moles of NO <sub>x</sub>
<i>N<sub>Pt cryst</sub></i>	number of Pt crystallites
<i>N<sub>Pt at</sub></i>	number of Pt atoms
<i>NS</i>	number of species <i>i</i> involved in the reduction
<i>N<sub>t</sub></i>	number of experimental data as function of time at a given <i>T</i>
<i>P<sub>Pt cryst</sub></i>	total perimeter of the Pt crystallites
<i>R</i>	gas constant
<i>R<sub>i</sub></i>	reaction rate of step <i>i</i> or net rate of production/consumption of species <i>i</i>
<i>S<sub>i</sub></i>	step <i>i</i>
<i>S<sub>0</sub></i>	sticking coefficient at 0 coverage
<i>t</i>	time
<i>T</i>	temperature
<i>x<sub>w</sub></i>	weight fraction
<i>y<sub>i</sub></i>	experimental value of kinetic datum <i>i</i>
<i>y<sub>i</sub><sup>mod</sup></i>	model prediction of kinetic datum <i>i</i>
<i>z</i>	reactor axial coordinate
<i>Z</i>	number of molecules in the unit cell

### Greek letters

$\Omega_{\text{Ba}(\text{NO}_3)_2}$	NO <sub>x</sub> adsorption capacity of the catalyst associated with Ba sites
$\Omega_{\text{Pt}}$	Pt catalyst capacity
$\alpha$	adaptive parameter in <i>E<sub>S5</sub></i>
$\alpha_V$	catalyst active Pt surface area
$\beta$	kinetic parameter after re-parameterization
$\varepsilon$	reactor void fraction
$\gamma$	adaptive parameter in <i>E<sub>S5</sub></i>
$\theta_i$	fractional coverage of surface species <i>i</i>
$\tau$	residence time
$\omega_i$	weight associated to species <i>i</i>

### Subscripts

act	active
ads	adsorption
at	atom
cryst	crystallite
des	desorption
<i>i</i>	index of gaseous and surface component
<i>j</i>	index of the reaction step
tot	total

gen and ammonia can be formed according to a parallel scheme via recombination of surface Pt-N species produced from dissociative adsorption of gaseous NO at metal Pt and via successive recombination of Pt-N and Pt-H species, respectively. However the selective catalytic reduction of NO<sub>x</sub> with ammonia and the oxidation of ammonia to give nitrogen are also considered in their scheme. Both Pihl et al. [8] and Ribeiro and co-workers [11] emphasise in their models the integral nature of the NO<sub>x</sub> Trap during regeneration so that a plug flow regeneration front and the associated concentration fronts of reactants and products develop, which travel along the reactor axis. They also assume the release of NO<sub>x</sub> from the trapping material in the gas phase as the first step in the process and note that it is not necessary to invoke a mechanism of surface diffusion of NO-containing species that are reduced at Pt. On the opposite Nova et al. [17] and Forzatti and Lietti [18] have shown that both H<sub>2</sub> and NH<sub>3</sub> can directly regenerate NO<sub>x</sub> stored onto Pt-Ba/Al<sub>2</sub>O<sub>3</sub> under nearly isothermal conditions via a Pt catalysed reaction that does not involve gaseous NO; they also suggest a two-steps reaction pathway involving the fast reaction of H<sub>2</sub> with stored NO<sub>x</sub> to give ammonia and the subsequent slower reaction of ammonia with stored NO<sub>x</sub> to give N<sub>2</sub>. Recently Lietti et al. [1,14] proposed that N<sub>2</sub> is formed exclusively via this in series two-steps pathway and also showed that the reduction of stored NO<sub>x</sub> with H<sub>2</sub> to give ammonia is much faster in the presence of water. The papers cited above convey a complex network of reactions of ammonia formation and utilisation in different zones of the reactor, where release of stored NO<sub>x</sub> to give NO/NO<sub>2</sub> in the gas phase and surface diffusion of NO-containing species are either assumed or disregarded.

In recent papers effluent measurements of different length catalyst sections [15] and intra catalyst measurements using spatially resolved inlet mass spectrometry (SpaciMS) [16] have been used to obtain a spatiotemporal resolution during Pt-Ba/Al<sub>2</sub>O<sub>3</sub> monolith LNT regeneration. On the other hand regeneration of stored NO<sub>x</sub> using a limited concentration of the reducing agent and with a purge of inert gas (e.g. He) in between the lean and the rich periods has been used in the laboratory to attain nearly isothermal conditions that prevent the thermal release of NO<sub>x</sub> in the gas phase and the associated greater complexity of network of reactions and to ensure a complete decoupling of storage and reduction chemistry [1,13,17].

A number of kinetic models of varying complexity have been developed in the literature to describe the regeneration of NO<sub>x</sub> Traps.

A detailed microkinetic model of NO<sub>x</sub> storage and reduction has been presented by Olsson et al. [20,21]. The model could describe NO<sub>x</sub> storage and regeneration with propene. The same group at Chalmers, in cooperation with the group at Cummins, has recently developed a detailed microkinetic model that describes NO<sub>x</sub> storage (NO<sub>x</sub> is allowed to be stored at two different types of sites) and reduction with H<sub>2</sub> in the presence of H<sub>2</sub>O and CO<sub>2</sub> over Pt-Ba/Al<sub>2</sub>O<sub>3</sub> monolith sample and also considers ammonia formation and consumption [22]. In this model the release at first of stored NO<sub>x</sub> in the gas phase is assumed to account for the NO<sub>x</sub> spike observed immediately upon switch from lean to rich conditions in commercial operation. Nitrogen is formed by reaction of two Pt-N species produced by NO decomposition at Pt sites and ammonia is formed by the reaction of P-N with Pt-H species, the last ones produced by dissociative adsorption of hydrogen. Ammonia is consumed to give N<sub>2</sub> by oxidation over Pt and by surface reaction with Ba nitrates and Ba nitrites. The parameters in the model are derived from kinetic gas theory, transition state theory, statistical thermodynamics, thermodynamic constraints, literature, experiments or are fitted to the experiments using least square methods. Microkinetic models were also developed by Xu et al. [23] and by Larson et al. [24] for the NO/H<sub>2</sub> gaseous reaction system using a commer-

high ratios of the reducing agent to NO<sub>x</sub> and lower temperatures; they noted that ammonia formed in one portion of the catalyst could be consumed in another portion of the catalyst via regeneration reactions or reduction of stored oxygen and emphasised the importance of slow sites. Ribeiro and co-workers [10,11] suggested that the regeneration of Pt-Ba/Al<sub>2</sub>O<sub>3</sub> monolith NO<sub>x</sub> Trap with hydrogen occurs through a complex pathway where at first nitro-

cial monolith NO<sub>x</sub> Trap catalyst. This model is relevant to real LNT operation under non-isothermal conditions where thermal decomposition of stored NO<sub>x</sub> is observed upon switch from lean to rich conditions. The model includes NO decomposition to N<sub>2</sub>O and N<sub>2</sub>, hydrogen reduction of adsorbed oxygen and OH groups to H<sub>2</sub>O, and the hydrogenation of N ad-atoms to NH<sub>3</sub>. In both these studies N<sub>2</sub> was not directly measured and was calculated assuming an instantaneous N atomic balance.

Koci and co-workers [25,26] developed a spatially distributed NSR model based on global kinetics for an industrial NSR catalyst of NM-Ba-CeO<sub>2</sub>/Al<sub>2</sub>O<sub>3</sub> type (NM: noble metal) involving rate expressions that include only gas-phase concentrations. The model of Koci et al. considered at first only the reduction of NO<sub>x</sub> by CO, H<sub>2</sub> and unburned hydrocarbons but was later extended to include the formation of NH<sub>3</sub> by reaction of H<sub>2</sub> with nitrates and the subsequent reaction of ammonia with oxygen, with NO<sub>x</sub> adsorbed on the catalyst surface and with NO from the gas phase, producing N<sub>2</sub>. Reaction kinetic parameters have been evaluated from a series of laboratory experiments collected over an industrial monolith sample and the model was validated over test bench measurements at Daimler. Global kinetic models were also developed by Tuttlies et al. [27], Olsson et al. [28,29], Sharma et al. [30,31] and Sholtz et al. [32] where the solid diffusion described by a shrinking core model and the presence of multiple storage sites are considered but ammonia formation and consumption are not included. Recently a global kinetic model was developed by Cao et al. [33] where it is assumed that the regeneration of the partially saturated monolith Pt-Ba/Al<sub>2</sub>O<sub>3</sub> catalyst using H<sub>2</sub> as the reducing agent involves the formation of NH<sub>3</sub> as intermediate from the stored NO<sub>x</sub> and that NH<sub>3</sub> acts as carrier of H atoms.

Along similar lines Clayton et al. [15,34] developed a simplified global kinetic model for NO<sub>x</sub> storage and reduction with hydrogen over a Pt-Ba/Al<sub>2</sub>O<sub>3</sub> monolith catalyst. The model assumes the existence of two different types of BaO sites on the catalyst, which differ in their storage as well as regeneration activity. The fast storage/reduction sites are conjectured to be in close proximity to the Pt/BaO interface, while the slow sites are far from the Pt sites. The reduction scheme considers the formation of ammonia from nitrates and its consumption by stored NO<sub>x</sub> to form N<sub>2</sub>. The global kinetic model was incorporated into a one-dimensional two phase transient model of the reactor to predict the spatiotemporal concentration profiles measured and the surface coverage calculated over a series of monoliths of progressively decreasing length under near isothermal conditions at a single temperature of 275 °C.

In the present paper regeneration data of LNT Pt-Ba/Al<sub>2</sub>O<sub>3</sub> catalyst in the powder form based on previous experimental work [1] are used to derive a kinetic model. Based on the reaction pathway pointed out in [1] and differently from other literature studies, the model is based exclusively on the consecutive reaction scheme with formation of ammonia from nitrates followed by reaction of ammonia with residual nitrates to give nitrogen, and consists of both elementary-like and lumped steps. The regeneration of the LNT Pt-Ba/Al<sub>2</sub>O<sub>3</sub> catalyst was accomplished using both H<sub>2</sub> and NH<sub>3</sub> as reducing agents to address the role of ammonia as intermediate in the regeneration with hydrogen. The regeneration was realised both in the presence and absence of water in the feed [1]. Here only the experiments realised in the presence of water are considered because in the absence of water a large induction period was observed that complicates the kinetic description of the reacting system. Finally the regeneration was accomplished under nearly isothermal conditions with limited concentration of H<sub>2</sub> and of NH<sub>3</sub> and with a He purge in between storage and regeneration periods to prevent thermal release of NO<sub>x</sub> and transients in the oxygen gas-phase concentration upon the lean-fuel rich switch. This differs from regeneration in commercial NO<sub>x</sub> traps where oxygen is present resulting in a significant temperature rise.

**Table 1**  
Catalyst characteristics.

Catalyst composition	BET surface area	Pt dispersion (H/Pt)	Mean dimension of Pt crystallites, $D_{\text{cryst}}$
Pt-Ba/Al <sub>2</sub> O <sub>3</sub> (1/20/100 w/w/w)	140 m <sup>2</sup> /g	0.55	2.0 nm

We show that the simple description of the regeneration scheme provided by the model is able to describe on a sound and quantitative basis the isothermal experimental data. The reactor model which incorporates the kinetic scheme based exclusively on the in series two steps pathway with ammonia as intermediate is validated against independent NH<sub>3</sub>- and H<sub>2</sub>-TPSR experiments. The model is also used to provide a spatiotemporal resolution of the LNT reactor during regeneration with ammonia.

## 2. Model development

### 2.1. Experimental data

The experiments that were used to develop the kinetic model were carried out in a quartz tubular fixed-bed micro-reactor using 60 mg of a Pt/BaO/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> (1/20/100, w/w/w) LNT catalyst sample in the powder form (100–150  $\mu$ m) [1]. The catalyst was prepared by successive impregnation of the  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> carrier calcined at 700 °C with aqueous solutions of Ba(CH<sub>3</sub>COO)<sub>2</sub> first and of Pt(NH<sub>3</sub>)<sub>2</sub>(NO<sub>2</sub>)<sub>2</sub> next after drying at 80 °C and calcination at 500 °C in between and final calcination at 500 °C for 5 h [1]. The Pt loading is 0.83% (w/w) and the metal dispersion, measured by hydrogen chemisorption at room temperature, is 55%. The BET surface area is around 140 m<sup>2</sup>/g and the Ba content of 16.5% (w/w) ensures an almost complete coverage of the alumina surface. The mean particle diameter of the Pt crystallites, calculated from Pt dispersion using the empirical relationship  $D_{\text{cryst}} (\text{nm}) = 1.1 / (\text{H/Pt})$  [35], is 2.0 nm, which compares well with that measured by HRTEM for another preparation batch of a catalyst with the same composition [36]. The characteristics of the catalyst are summarised in Table 1.

After catalyst conditioning, realised by performing few adsorption/regeneration cycles with NO/O<sub>2</sub> (1000 ppm NO and 3% (v/v) O<sub>2</sub> in He) and H<sub>2</sub> (2000 ppm in He) at 350 °C with an inert purge (He) between the two phases, NO<sub>x</sub> were adsorbed at the same temperature of 350 °C. The NO<sub>x</sub> storage was accomplished by imposing a rectangular step feed of NO (1000 ppm) in flowing He + 3% (v/v) O<sub>2</sub> for about 400 s, followed by a He purge to provoke the desorption of weakly adsorbed species. The temperature of 350 °C and the duration of the storage phase guarantee that at the beginning of the regeneration phase stored NO<sub>x</sub> are present primarily in the form of nitrates [18], as also revealed by FTIR experiments [37], and that the surface coverage of nitrates is close to saturation and it can be assumed as almost constant along the axis of the reactor.

In the experiments used to develop the kinetic model the reduction of NO<sub>x</sub> stored at 350 °C was accomplished at four *T* values between 150 and 350 °C. During He purge after NO<sub>x</sub> adsorption at 350 °C the catalyst temperature was set to the desired level and then, after stabilisation of the Mass Spec signals, H<sub>2</sub> (2000 ppm in He + 1% H<sub>2</sub>O, v/v) or NH<sub>3</sub> (1000 ppm in He + 1% H<sub>2</sub>O, v/v) were admitted in a step-wise manner. A complete decoupling of the storage and of the reduction phases was achieved by applying an He purge in between the two phases. Besides, the transients in the oxygen gas-phase concentration upon the lean-rich switch, with the associated undesired reactions of complete oxidation, were avoided. Moreover isothermal conditions were realised in the catalyst bed, due to the small concentration of H<sub>2</sub> or NH<sub>3</sub> employed during regeneration. Accordingly the thermal decomposition of

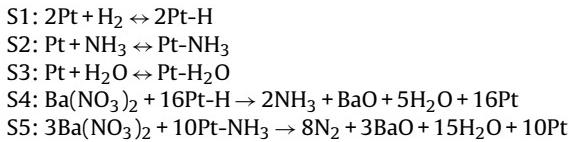
surface nitrates was prevented and the chemistry of Pt catalysed  $\text{NO}_x/\text{H}_2$  and  $\text{NO}_x/\text{NH}_3$  gas mixtures could be neglected in the kinetic scheme with a significant simplification of the reaction network. Then, when the reduction process was completed, the  $\text{H}_2$  and  $\text{NH}_3$  flow was stopped, the catalyst was heated at 350 °C under He atmosphere and the amounts of residual stored  $\text{NO}_x$  was then estimated by reduction at this temperature with  $\text{H}_2$  or with  $\text{NH}_3$ , respectively.

Different TPSR experiments were used for the validation of the kinetic model. In these experiments after storage at 350 °C and cooling in He down to room temperature the reduction of stored  $\text{NO}_x$  was accomplished under a reducing atmosphere (2000 ppm  $\text{H}_2$  in He + 1%  $\text{H}_2\text{O}$ , v/v, 1000 ppm  $\text{H}_2$  in He + 1%  $\text{H}_2\text{O}$ , v/v, 2200 ppm  $\text{NH}_3$  in He + 1%  $\text{H}_2\text{O}$ , v/v and 550 ppm  $\text{NH}_3$  in He + 1%  $\text{H}_2\text{O}$ , v/v) with an heating rate of 10 °C/min up to 500 °C.

Preliminary experiments, where a step-wise change in the feed ammonia concentration (from 0 to 1000 ppm) was applied to the empty micro-reactor (i.e. a reactor with no catalyst but with all else), showed an ammonia “time delay” that was described by  $\text{NH}_3$  adsorption-desorption onto the Mass Spec capillary line kept at 90 °C.

## 2.2. Kinetic model

In this section a kinetic model is developed to describe the reduction of stored nitrates by  $\text{H}_2$  and  $\text{NH}_3$  in the presence of water. In order to explain the product distribution the following sequence of steps is considered:



Elementary-like steps S1–S3 describe the adsorption-desorption of hydrogen, ammonia and water at Pt site respectively. Steps S4 and S5 describe in a lumped manner the reduction of stored nitrates by hydrogen to give ammonia and the reduction of stored nitrates by ammonia to give nitrogen respectively, and account for the products observed in the reaction system. Notice that BaO in steps S4 and S5 can be transformed in the presence of water into  $\text{Ba}(\text{OH})_2$  according to the reaction:  $\text{BaO} + \text{H}_2\text{O} \rightarrow \text{Ba}(\text{OH})_2$ .

The reduction either by hydrogen or by ammonia of Pt-O remaining on the catalyst surface after lean  $\text{NO}_x$  storage followed by He purge is neglected. Indeed the amount of PtO sites is small relative to the consumption of reductants via the other reactions. Besides this reaction is considered to be very fast at any temperature, so that it is completed in less than 10 s. Accordingly it does not affect to any significant extent the dynamics of the reduction process.

The rate expressions for each step are given in Table 2. The kinetic parameters in the rate equation of adsorption of species  $i$  in step  $j$  are given by:

$$k_{\text{ads},j} = S_{i,0} (2\pi M_i / T / R)^{0.5} \times \alpha_V$$

**Table 3**  
Kinetic parameters taken from the literature.

Step	Sticking coefficient, $S_{i,0}$	Rate constant of adsorption, $k_{\text{ads},i}$ ( $\text{s}^{-1}$ )	Pre-exponential factor, $k^0_{\text{des},i}$ ( $\text{s}^{-1}$ )	Desorption energy, $E_{\text{des},i}$ (kJ/mol)	Reference
S1	0.046	$1.948 \times 10^4$	$3.690 \times 10^{21}$	67.0	[38]
S2	1	$1.331 \times 10^5$	$[3.032 \times 10^8]$	48.4	[39]
S3	0.75	$9.705 \times 10^4$	$1.794 \times 10^{14}$	40.3	[38]

**Table 2**  
Rate expressions for each of the steps of the kinetic model.

Reaction step j	Rate expression
S1	$R_{S1} = k_{\text{ad},\text{H}_2} \times \theta_{\text{Pt}}^2 \times C_{\text{H}_2} - k_{\text{des},\text{H}_2} \times \theta_{\text{Pt-H}_2}$
S2	$R_{S2} = k_{\text{ads},\text{NH}_3} \times \theta_{\text{Pt}} \times C_{\text{NH}_3} - k_{\text{des},\text{NH}_3} \times \theta_{\text{Pt-NH}_3}$
S3	$R_{S3} = k_{\text{ads},\text{H}_2\text{O}} \times \theta_{\text{Pt}} \times C_{\text{H}_2\text{O}} - k_{\text{des},\text{H}_2\text{O}} \times \theta_{\text{Pt-H}_2\text{O}}$
S4	$R_{S4} = k_4 \times \Omega_{\text{Ba}(\text{NO}_3)_2} \theta_{\text{Ba}(\text{NO}_3)_2} \times \theta_{\text{Pt-H}}$
S5	$R_{S5} = k_5 \times \Omega_{\text{Ba}(\text{NO}_3)_2} \theta_{\text{Ba}(\text{NO}_3)_2} \times \theta_{\text{Pt-NH}_3}$

$$k_{\text{des},j} = k_{\text{des},j}^0 \exp \left( \frac{-E_{\text{des},j}}{RT} \right)$$

with  $i = \text{H}_2, \text{NH}_3$  and  $\text{H}_2\text{O}$  and  $j = \text{S1}, \text{S2}, \text{S3}$ .  $S_{i,0}$  is the sticking coefficient,  $M_i$  the molecular weight of species  $i$ ,  $\alpha_V$  the catalyst active Pt surface area (see Table 1), and  $R$  the gas constant. The kinetic constants  $k_j$  of the reaction rate of step  $j = \text{S4}, \text{S5}$  are described by the Arrhenius expression:

$$k_j = k_j^0 \exp \left( \frac{-E_j}{RT} \right)$$

where  $k_j^0$  and  $E_j$  are the corresponding pre-exponential coefficient and the activation energy. The rate expressions for the lumped processes S4 and S5 in Table 2 assume that the first reduction step of nitrates by adsorbed hydrogen (Pt-H) or adsorbed ammonia (Pt-NH<sub>3</sub>), respectively is rate determining and accordingly show a first order dependence on the surface concentration of  $\text{Ba}(\text{NO}_3)_2$  ( $\Omega_{\text{Ba}(\text{NO}_3)_2} \theta_{\text{Ba}(\text{NO}_3)_2}$ ) and on either  $\theta_{\text{Pt-H}}$  and  $\theta_{\text{Pt-NH}_3}$ .  $\Omega_{\text{Ba}(\text{NO}_3)_2}$  is the  $\text{NO}_x$  adsorption capacity of the catalyst associated with Ba sites (mol/m<sup>3</sup><sub>cat</sub>) and  $\theta_i$  is the fractional coverage of surface species  $i$  ( $i = \text{Ba}(\text{NO}_3)_2, \text{P-H}, \text{Pt-NH}_3$ ).

The adsorption-desorption of hydrogen, ammonia and water on Pt have been widely studied and the rate constants of steps S1, S2 and S3 were taken from literature and are given in Table 3. The parameter in brackets in Table 3 was not retained in the kinetic study and was estimated by regression to the experimental data of reduction of nitrates with ammonia to help predict certain trends in the experimental data, as also done elsewhere [23].

## 2.3. Reactor model

The experimental data collected over the powder catalyst were analysed according to a dynamic 1-D isothermal pseudo-homogeneous plug flow model of the laboratory micro-reactor. On the basis of diagnostic criteria the influence of both intra-particle catalyst gradients and external mass transfer limitations were found negligible. Under these hypotheses the unsteady mass balances for gas species ( $\text{H}_2, \text{NH}_3, \text{N}_2, \text{H}_2\text{O}$ ) are given below:

$$(H_2) \quad \begin{aligned} \varepsilon \frac{\partial C_{\text{H}_2}}{\partial t} &= -\frac{1}{\tau} \frac{\partial C_{\text{H}_2}}{\partial z} + (1-\varepsilon) R_{\text{H}_2} \\ R_{\text{H}_2} &= -R_{\text{S1}} \end{aligned}$$

$$(NH_3) \quad \begin{aligned} \varepsilon \frac{\partial C_{\text{NH}_3}}{\partial t} &= -\frac{1}{\tau} \frac{\partial C_{\text{NH}_3}}{\partial z} + (1-\varepsilon) R_{\text{NH}_3} \\ R_{\text{NH}_3} &= -R_{\text{S2}} + 2R_{\text{S4}} \end{aligned}$$

$$(N_2) \quad \varepsilon \frac{\partial C_{N_2}}{\partial t} = -\frac{1}{\tau} \frac{\partial C_{N_2}}{\partial z} + (1-\varepsilon) R_{N_2}$$

$$R_{N_2} = -8R_{S5}$$

$$(H_2O) \quad \varepsilon \frac{\partial C_{H_2O}}{\partial t} = -\frac{1}{\tau} \frac{\partial C_{H_2O}}{\partial z} + (1-\varepsilon) R_{H_2O}$$

$$R_{H_2O} = -R_{S3} + 5R_{S4} + 15R_{S5}$$

where  $C_i$  is the gas phase concentration of species  $i$ ,  $R_i$  the net rate of reaction of species  $i$  ( $i = H_2, N_2, NH_3, H_2O$ ),  $z$  the non-dimensional reactor axial coordinate,  $\tau$  the residence time,  $\varepsilon$  the reactor void fraction and  $t$  is time. The unsteady mass balances for surface species ( $Ba(NO_3)_2, BaO, Pt, Pt-H, Pt-NH_3, Pt-H_2O$ ) are given below:

$$(Ba(NO_3)_2) \quad \Omega_{Ba(NO_3)_2} \frac{\partial \theta_{Ba(NO_3)_2}}{\partial t} = R_{Ba(NO_3)_2}$$

$$R_{Ba(NO_3)_2} = -R_{S4} - 3R_{S5}$$

$$(BaO) \quad \Omega_{Ba(NO_3)_2} \frac{\partial \theta_{BaO}}{\partial t} = R_{BaO}$$

$$R_{BaO} = R_{S4} + 3R_{S5}$$

$$(Pt) \quad \Omega_{Pt} \frac{\partial \theta_{Pt}}{\partial t} = R_{Pt}$$

$$R_{Pt} = -2R_{S1} - R_{S2} - R_{S3} + 16R_{S4} + 10R_{S5}$$

$$(Pt-H) \quad \Omega_{Pt} \frac{\partial \theta_{Pt-H}}{\partial t} = R_{Pt-H}$$

$$R_{Pt-H} = 2R_{S1} - 16R_{S4}$$

$$(Pt-NH_3) \quad \Omega_{Pt} \frac{\partial \theta_{Pt-NH_3}}{\partial t} = R_{Pt-NH_3}$$

$$R_{Pt-NH_3} = R_{S2} - 10R_{S5}$$

$$(Pt-H_2O) \quad \Omega_{Pt} \frac{\partial \theta_{Pt-H_2O}}{\partial t} = R_{Pt-H_2O}$$

$$R_{Pt-H_2O} = R_{S3}$$

$\Omega_{Ba(NO_3)_2}$  has already been defined as the  $NO_x$  adsorption capacity of the catalyst associated with Ba sites,  $\Omega_{Pt}$  is the catalyst Pt surface capacity ( $mol/m^2_{cat}$ ),  $\theta_i$  and  $R_i$  are the surface coverage and the net rate of reaction of catalyst surface species  $i$  ( $i = BaO, Ba(NO_3)_2, Pt, Pt-H, Pt-NH_3, Pt-H_2O$ ), and  $t$  is time.

$\Omega_{Ba(NO_3)_2}$  is calculated from the moles of  $NO_x$  stored during the lean phase and differs slightly among the set of experiments considered in the present study. The N-balance, estimated by comparing the amounts of  $NO_x$  adsorbed during the lean phase with those of the N-containing species formed both on reduction at the investigated temperature and on the final reduction at  $350^\circ C$  with the same reducing agent (i.e.  $H_2$  or  $NH_3$ ), always closed within  $\pm 5\%$ .  $\Omega_{Pt}$  was calculated from  $H_2$  chemisorption measurements at room temperature (see Section 2). Accordingly these two parameters were not fitted to the experimental data.

The initial and boundary conditions are specified below and include zero concentration of the reducing agent (either  $H_2$  or  $NH_3$ ) at time zero at any axial position in the reactor and constant concentration of the same reducing agent at any time at the inlet of the reactor, after the stepwise increase. Also the concentration of water is equal to 1% (v/v) at the entrance of the reactor at any time and is constant along the reactor axis at time zero. Besides the fractional coverage of the surface species along the axial position of the reactor is uniform at time zero.

$$C_i(0, z) = C_{i,t_0} \quad (i = H_2, NH_3, H_2O)$$

$$C_i(t, 0) = C_{i,z_0} \quad (i = H_2, NH_3, H_2O)$$

$$\theta_i(0, z) = \theta_{i,t_0} \quad (i = BaO, Ba(NO_3)_2, Pt, Pt-H, Pt-NH_3, Pt-H_2O)$$

The delay of ammonia (see Section 2) is accounted for by a PFR model where  $NH_3$  adsorption–desorption takes place onto the Mass Spec capillary walls at  $90^\circ C$  ( $T$  set of the MS capillary) and in series to the catalytic laboratory micro-reactor. The dynamics of  $NH_3$  adsorption–desorption in the Mass Spec capillary was calculated from preliminary experiments.

The energy balance equations are not incorporated in the model because of the isothermal conditions of the experimental data.

The reactor model consists of 10 PDEs and was solved numerically using the method of lines. The axial reactor length was split into 25 grid points and in each point the spatial derivates were approximated by the Eulero backward differentiation method. Thus from a 10 PDEs problem a 250 grid points ODEs system was obtained and solved using the BzzMath 6.0 library [40].

The four experiments where the reduction of stored  $NO_x$  was accomplished with ammonia at constant temperature at 150, 200, 250 and  $300^\circ C$  were used to estimate the parameters of step S5 and  $k_{des, NH_3}^0$ . Then these parameters were fixed to the values of this regression and the other two parameters  $k_4^0$ , and  $E_4$  were estimated by regression to the set of four experiments where the reduction of stored  $NO_x$  was accomplished with hydrogen at 150, 200, 250 and  $350^\circ C$ .

The adaptive kinetic parameters were estimated by minimising the weighted residual sum of squares between experimental values and model predictions for the complete data set [41]:

$$\min_b \sum_{i=1}^{NS} \left( \sum_{j=1}^{Nt} \omega_i (y_{i,j}^{exp} - y_{i,j}^{mod}(b))^2 \right)$$

where NS is the number of species ( $i$ ) involved in the reduction,  $Nt$  is the number of experimental data as function of the time,  $\omega_i$  is the weight associated to species  $i$ ,  $b$  is the vector that contain the adaptive parameters of the model.

Re-parameterization was made to reduce the strong correlation between the pre-exponential factor and the activation energy, as given below:

$$\beta_1^{des,i} = \ln(k_{des,i}^0) \quad \beta_1^i = \ln(k_j^0)$$

$$\beta_2^{des,i} = \frac{-E_{des,i}}{R} \quad \beta_2^i = \frac{-E_j}{R}$$

$$k_{des,i} = \exp \left[ \beta_1^{des,i} + \frac{\beta_2^{des,i}}{T} \right] \quad k_j = \exp \left[ \beta_1^i + \frac{\beta_2^i}{T} \right]$$

### 3. Results and discussion

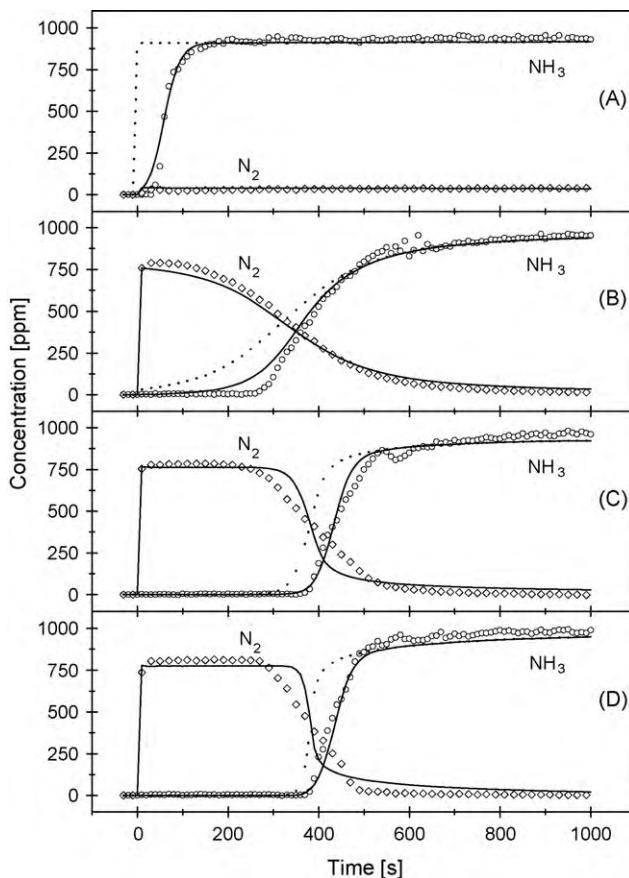
#### 3.1. Reduction of stored $NO_x$ with $NH_3$

Fig. 1 shows the experimental concentration of effluent  $NH_3$  and of effluent  $N_2$  at the MS quadrupole detector (open symbols) during the reduction of stored nitrates with ammonia at four different temperatures. At  $150^\circ C$  (panel A) only a limited consumption of ammonia and a small concentration of nitrogen are measured. At higher temperatures ( $200^\circ C$  in panel B,  $250^\circ C$  in panel C and  $300^\circ C$  in panel D) and at the beginning of the regeneration phase the process is always limited by the concentration of the reducing agent and ca 800 ppm of nitrogen are produced. At higher regeneration times a decrease in the effluent nitrogen concentration is observed, which anticipates the ammonia breakthrough due to delay of the effluent ammonia concentration associated with  $NH_3$  adsorption–desorption in the capillary of the Mass Spectrometer.

**Table 4**

Moles of nitrates stored at 350 °C consumed during the reduction at different temperatures.

Reducing agent	T (°C)	Reduction time (s)	NO <sub>x</sub> reduced at given time (mol/g <sub>cat</sub> )	NO <sub>x</sub> reduced at the given T + at 350 °C (mol/g <sub>cat</sub> )	NO <sub>x</sub> reduction efficiency (%)
NH <sub>3</sub>	150	1000	3.468 × 10 <sup>-5</sup>	2.268 × 10 <sup>-4</sup>	–
		4860	1.313 × 10 <sup>-4</sup>	58	–
	200	1000	2.723 × 10 <sup>-4</sup>	2.989 × 10 <sup>-4</sup>	–
		1560	2.755 × 10 <sup>-4</sup>	92	–
	250	1000	2.921 × 10 <sup>-4</sup>	2.963 × 10 <sup>-4</sup>	–
		1430	2.927 × 10 <sup>-4</sup>	99	–
		1000	2.905 × 10 <sup>-4</sup>	2.936 × 10 <sup>-4</sup>	–
H <sub>2</sub>	150	1000	2.909 × 10 <sup>-4</sup>	99	–
		1750	2.695 × 10 <sup>-4</sup>	3.082 × 10 <sup>-4</sup>	–
	200	1000	2.875 × 10 <sup>-4</sup>	3.040 × 10 <sup>-4</sup>	–
		1480	2.995 × 10 <sup>-4</sup>	99	–
	250	1000	3.103 × 10 <sup>-4</sup>	3.267 × 10 <sup>-4</sup>	–
		1450	3.252 × 10 <sup>-4</sup>	100	–
		815	2.818 × 10 <sup>-4</sup>	100	100



**Fig. 1.** Isothermal reduction with NH<sub>3</sub> of NO<sub>x</sub> stored at 350 °C: (A) T = 150 °C; (B) T = 200 °C; (C) T = 250 °C; (D) T = 300 °C. Experimental concentration of NH<sub>3</sub> and N<sub>2</sub> at the MS detector, open symbols; model prediction of effluent concentration of NH<sub>3</sub> and N<sub>2</sub> at the MS detector, full lines; model prediction of effluent concentration of NH<sub>3</sub> at the reactor exit, dashed line. The inlet concentration of NH<sub>3</sub> is set at 1000 ppm at t = 0.

On increasing the reduction temperature the decrease in nitrogen concentration and the corresponding NH<sub>3</sub> breakthrough curves are observed later and become steeper due to the higher rate of reaction. At the given temperature, as the regeneration proceeds further with time, the concentration of nitrogen drops to zero and the NH<sub>3</sub> concentration approaches the inlet value showing that the reduction process is complete.

From these experiments and the final reduction run accomplished thereafter at 350 °C it is possible to calculate for each temperature the moles of NO<sub>x</sub> reduced by NH<sub>3</sub> to form nitrogen (after the time period of 1000 s shown in Fig. 1 and till the end of the experiment) and also the sum of these moles with those that are reduced at 350 °C; these last ones correspond the moles of NO<sub>x</sub> previously stored onto the catalyst at 350 °C. These quantities are listed in Table 4. In the same table the reduction efficiency at the end of the isothermal experiment, defined as the ratio between the moles of NO<sub>x</sub> reduced at a given temperature to the sum of these moles with those that are reduced thereafter at 350 °C, is also given. The stored NO<sub>x</sub> that are involved in the reduction process increase with temperature, particularly in the range 150–200 °C, and the reduction efficiency approaches 100% only at T ≥ 200 °C. This clearly demonstrates that nitrates with different reactivity are present at the catalyst surface and that less reactive sites take part in the reaction only at T ≥ 200 °C but not at 150 °C. The more and less reactive nitrates are envisaged as close and far from the noble metal, respectively, although some authors assume bulk Ba nitrates where the outer layer is more reactive than Ba sites residing within the particle [3,27].

In order to account for the participation of Ba nitrates with different reactivity in the reduction with ammonia the energy of activation of step S5 was assumed to depend on the surface concentration of Ba-nitrates according to the following sigmoid function:

$$(E_{S5}) \quad E_{S5} = E_{\text{MIN}} + \frac{[E_{\text{MAX}} - E_{\text{MIN}}]}{[1 + \exp(\alpha(\Omega_{\text{Ba}(\text{NO}_3)}\theta_{\text{Ba}(\text{NO}_3)} - \gamma))]}$$

where E<sub>MIN</sub> and E<sub>MAX</sub> represent the minimum and maximum values of the energy of activation at the maximum and nil concentration

**Table 5**

Values of the parameter estimates for the reduction of stored NO<sub>x</sub> with NH<sub>3</sub> and with H<sub>2</sub>.

Step	Pre-exponential factor, k <sub>4</sub> <sup>0</sup> (mol/m <sup>-3</sup> s <sup>-1</sup> )	Activation energy, E <sub>4</sub> (kJ/mol)
S4	3.45 × 10 <sup>6</sup>	22.94
Step	k <sub>5</sub> <sup>0</sup> (mol/m <sup>3</sup> s <sup>-1</sup> )	E <sub>att MIN</sub> (kJ/mol)
S5	1.26 × 10 <sup>10</sup>	116.7
		E <sub>att MAX</sub> (kJ/mol)
		α
		β
		23.2

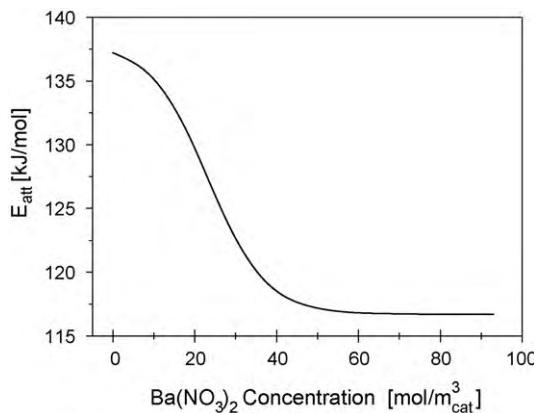


Fig. 2. Dependence of  $E_{\text{att}}$  of step S5 from  $\text{Ba}(\text{NO}_3)_2$  concentration.

of  $\text{Ba}(\text{NO}_3)_2$  respectively,  $\alpha$  and  $\gamma$  are adaptive parameters that account for the slope and the position of the inflection point of the sigmoid curve.

The model predictions (full lines) and the experimental effluent concentrations at the MS detector (open symbols) are compared in Fig. 1. It is observed that the breakthrough time of  $\text{NH}_3$  is predicted quite well by the model at any temperature; only at  $200^\circ\text{C}$  the slope associated with the actual  $\text{NH}_3$  concentration trace is somehow sharper and the breakthrough time is slightly longer than predicted by the model. The delay of the effluent ammonia concentration can be appreciated by comparing the concentration of ammonia predicted by the model at the MS detector (full lines) and at the reactor exit (dashed lines). At  $150^\circ\text{C}$  the breakthrough of effluent ammonia, which here is due primarily to the time delay, disappears and at higher temperatures the concentration of ammonia at the reactor exit always anticipates that observed in the effluent stream at the MS and corresponds to the decrease in the concentration of nitrogen.

The values of the parameter estimates obtained by regression are reported in Table 3 for steps S1, S2 and S3, and in Table 5 for step S5. The dependence of  $E_{\text{S5}}$  from the surface concentration of  $\text{Ba}(\text{NO}_3)_2$  is shown in Fig. 2. The energy of activation of step S5 is almost constant at the level of  $117 \text{ kJ/mol}$  from ca  $93 \text{ mol Ba}(\text{NO}_3)_2/\text{m}^3_{\text{cat}}$  down to ca  $60 \text{ mol Ba}(\text{NO}_3)_2/\text{m}^3_{\text{cat}}$ , and then increases progressively up to  $137 \text{ kJ/mol}$  at  $\text{mol Ba}(\text{NO}_3)_2/\text{m}^3_{\text{cat}} = 0$ . The change from  $93$  to  $60 \text{ mol Ba}(\text{NO}_3)_2/\text{m}^3_{\text{cat}}$  corresponds to the consumption of ca  $1 \times 10^{-4} \text{ mol NO}_x/\text{g}_{\text{cat}}$  that represents the amount of most reactive  $\text{NO}_x$  species.

From the physico-chemical characteristics of the catalyst it is possible to compute the quantity of  $\text{NO}_x$  species surrounding the Pt crystallites. Based on the mean dimension of the Pt crystallites given in Table 1 ( $D_{\text{Pt cryst}} = 20 \text{ \AA}$ ), the characteristics of the unit cell of Pt with the FCC structure ( $a_{\text{Pt}} = 3.9 \text{ \AA}$ ;  $Z_{\text{Pt}} = 4$ ) [JCPDS 4-802] and further assuming that the Pt crystallites have a hemispherical shape the number of Pt atoms per crystallite,  $N_{\text{Pt at/cryst}}$ , is obtained as:

$$\frac{N_{\text{Pt at}}}{\text{cryst}} = \frac{2}{3} \pi \left( \frac{D_{\text{Pt cryst}}}{2} \right)^3 \times \frac{1}{(a_{\text{Pt}}^3)} Z_{\text{Pt}} = 141$$

The following number of Pt atoms per g of catalyst,  $N_{\text{Pt at/g}_{\text{cat}}}$ , is also calculated:

$$\frac{N_{\text{Pt at}}}{\text{g}_{\text{cat}}} = \left[ \frac{x_{\text{w Pt}}}{M_{\text{Pt}}} \right] N_{\text{Av}} = 2.564 \times 10^{19}$$

Here  $x_{\text{w Pt}}$  represents the catalyst weight fraction of Pt,  $M_{\text{Pt}}$  is the molecular weight of Pt, and  $N_{\text{Av}}$  is the Avogadro number. Next the number of crystallites per g of catalyst,  $N_{\text{Pt cryst/g}_{\text{cat}}}$ , is obtained

using the following relation:

$$\frac{N_{\text{Pt cryst}}}{\text{g}_{\text{cat}}} = N_{\text{Pt at/g}_{\text{cat}}} / N_{\text{Pt at/cryst}} = 1.816 \times 10^{17}$$

and the total perimeter of Pt crystallites per g of catalyst,  $P_{\text{Pt cryst/g}_{\text{cat}}}$ , is calculated:

$$\frac{P_{\text{Pt cryst}}}{\text{g}_{\text{cat}}} = \pi D_{\text{Pt cryst}} \times \frac{N_{\text{Pt cryst}}}{\text{g}_{\text{cat}}} = 1.14 \times 10^{19}$$

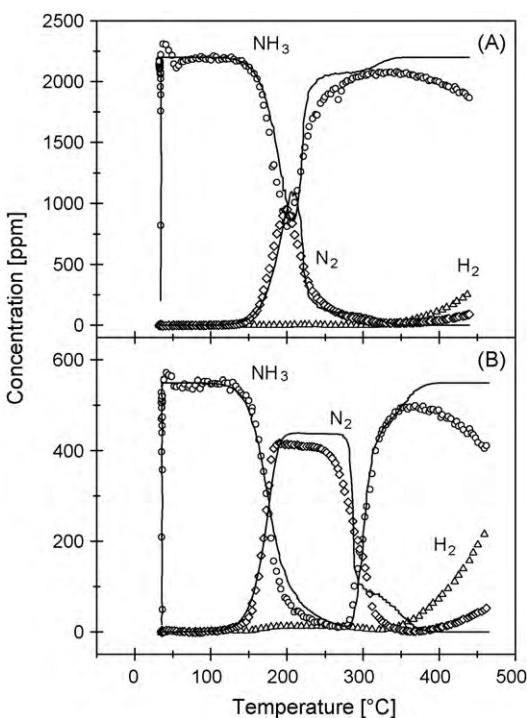
Finally on the basis of the unit cell characteristics of  $\text{Ba}(\text{NO}_3)_2$  with the FCC structure ( $a_{(\text{Ba}(\text{NO}_3)_2)} = 8.12 \text{ \AA}$ ;  $Z_{(\text{Ba}(\text{NO}_3)_2)} = 4$ ) [JCPDS 24-53], and assuming that the Ba content ensures the complete coverage of the alumina surface in the catalyst the total number of moles of  $\text{NO}_x$  species per g of catalyst, that surround the Pt crystallites as first neighbours,  $N_{\text{NO}_x}/\text{g}_{\text{cat}}$ , is obtained as follows:

$$\begin{aligned} \frac{N_{\text{NO}_x}}{\text{g}_{\text{cat}}} &= P_{\text{Pt cryst}}/\text{g}_{\text{cat}} / a_{(\text{Ba}(\text{NO}_3)_2)} \times Z_{(\text{Ba}(\text{NO}_3)_2)} \times \frac{2}{N_{\text{Av}}} \\ &\quad \times \frac{D_{\text{Pt cryst}} + a_{(\text{Ba}(\text{NO}_3)_2)}}{D_{\text{Pt cryst}}} = 2.64 \times 10^{-5} \text{ mol NO}_x/\text{g}_{\text{cat}} \end{aligned}$$

The assumption of a complete coverage of the alumina surface by  $\text{BaO}$  is in line with earlier findings by Castoldi et al. [6] and with the disappearance of the FTIR bands of alumina surface OH groups. The term  $((D_{\text{Pt cryst}} + a_{(\text{Ba}(\text{NO}_3)_2)})/D_{\text{Pt cryst}})$  accounts for the geometrical coupling between the perimeter of the Pt crystallite and the unit cell of  $\text{Ba}(\text{NO}_3)_2$ . When the particle diameter distribution of the Pt crystallites is taken into account (e.g.  $20 \pm 5 \text{ \AA}$ ) and the second neighbours to Pt crystallites are also considered,  $N_{\text{NO}_x}/\text{g}_{\text{cat}}$  becomes very close to the moles of the most reactive  $\text{NO}_x$  species provided by the kinetic study (near  $1 \times 10^{-4} \text{ mol/g}_{\text{cat}}$ ). This eventually confirms the association of the most reactive  $\text{Ba}(\text{NO}_3)_2$  species, that are reduced by ammonia already at  $150^\circ\text{C}$ , with those in close proximity to the Pt crystallites (i.e. first and second neighbours) and the association of the less reactive ones, that are reduced only at  $T \geq 200^\circ\text{C}$ , with those far from the Pt crystallites.

To explain the participation in the reduction process of less reactive  $\text{Ba}(\text{NO}_3)_2$ , i.e. of the species far from Pt, reverse spill-over of  $\text{NO}_x$  species on the surface of the  $\text{BaO}/\text{Ba}(\text{OH})_2$  phase and across the  $\text{Pt-BaO}/\text{Ba}(\text{OH})_2$  interface is likely involved, in line with previous literature indication [3,42,43]. In this case the role of the reductant is to keep Pt in a reduced state. It is noted that the reduction of stored  $\text{NO}_x$  does not occur to an appreciable extent over  $\text{BaO}/\text{Al}_2\text{O}_3$  at any temperature [17] while  $\text{NO}_x$  stored far from Pt are effectively reduced at low temperature ( $150^\circ\text{C}$ ) with  $\text{H}_2$  (see below) but not with ammonia. Accordingly the nature of reducing agent does affect the reduction of metal sites and/or the mobility of the stored  $\text{NO}_x$  species. Still the involvement of hydrogen spillover (after activation of  $\text{H}_2$  on Pt sites) toward nitrate adspecies cannot be excluded, although these aspects deserve further investigations.

The most reactive Ba sites in close proximity to Pt crystallites are regenerated at first during reduction but are saturated at first during  $\text{NO}_x$  storage as well. The less reactive Ba sites are involved later on after the most reactive sites have been either regenerated during reduction or occupied during  $\text{NO}_x$  storage. Indeed it has been shown that the most effective pathway for  $\text{NO}_x$  storage from  $\text{NO}/\text{O}_2$  is represented by the stepwise oxidation of  $\text{NO}$  followed by adsorption at a Ba site in proximity of the Pt site leading to the formation of nitrite adsorbed species (nitrite route) [37]. Nitrites are then progressively transformed into nitrates that are predominant at catalyst saturation [37,44]. Oxidation of  $\text{NO}$  to  $\text{NO}_2$  by gaseous oxygen can also occur; the  $\text{NO}_2$  so formed can be stored on  $\text{BaO}$  either close to or far from the Pt site directly in the form of nitrates according to a disproportion reaction to give Ba-nitrates and  $\text{NO}$  (nitrate route):  $3\text{NO}_2 + \text{BaO} \rightarrow \text{Ba}(\text{NO}_3)_2 + \text{NO}$ . As nitrites are



**Fig. 3.** NH<sub>3</sub>-TPSR runs performed with 1% H<sub>2</sub>O in the feed after NO<sub>x</sub> adsorption at 350 °C: (A) 2200 ppm of NH<sub>3</sub>; (B) 550 ppm of NH<sub>3</sub>. Experimental effluent concentration of NH<sub>3</sub>, N<sub>2</sub> and H<sub>2</sub> at the MS detector, open symbols; model prediction of effluent concentrations of NH<sub>3</sub>, N<sub>2</sub> and H<sub>2</sub> at the MS detector, full lines.

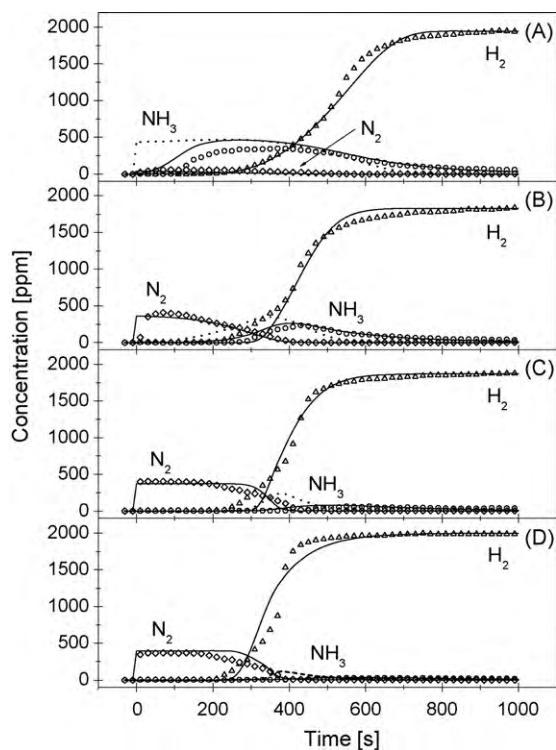
the most abundant species before NO<sub>x</sub> breakthrough [37,44] and at low temperature [18] the nitrite pathway is believed to dominate over the nitrate pathway. It is noted that the nitrite route involves adsorption only at Ba sites in close proximity to the Pt crystallites while the nitrate route on the opposite can involve in principle Ba sites either close or far from the Pt crystallites. However since the former Ba sites have been already involved in the fast nitrite pathway the latter ones are believed to be preferentially involved in the nitrate route.

The model of the reduction of stored NO<sub>x</sub> by NH<sub>3</sub> was validated without any adjustment of the parameter estimates by comparing experimental data collected during TPSR runs performed with 550 and 2200 ppm of NH<sub>3</sub> with 1% H<sub>2</sub>O in the feed with model predictions (Fig. 3). The results shown in Fig. 3 demonstrate a very nice agreement between experimental data and model predictions. The apparent disagreement observed above 350 °C is due to ammonia decomposition into H<sub>2</sub> and N<sub>2</sub>, which is not accounted for in the model.

### 3.2. Reduction of stored NO<sub>x</sub> with H<sub>2</sub>

The experiments where the reduction of NO<sub>x</sub> stored at 350 °C was accomplished with hydrogen at 150, 200, 250 and 350 °C were used to estimate the parameters  $k_4^0$  and  $E_4$  while the parameters of step S5 and  $k_{\text{des}, \text{NH}_3}^0$  were fixed to the values given in Tables 3 and 5.

Fig. 4 shows the experimental concentration of effluent H<sub>2</sub> and of the effluent products (NH<sub>3</sub> and N<sub>2</sub>) at the MS detector during the reduction of stored nitrates with hydrogen at different temperatures. At low temperature (150 °C in panel A) and at the beginning of the regeneration phase the consumption of hydrogen is complete and the reaction is controlled by the concentration of hydrogen, which indicates that hydrogen is more reactive than ammonia towards surface nitrates. Only NH<sub>3</sub> is observed among the products, which indicates that step S4 (reaction of nitrates with H<sub>2</sub> to



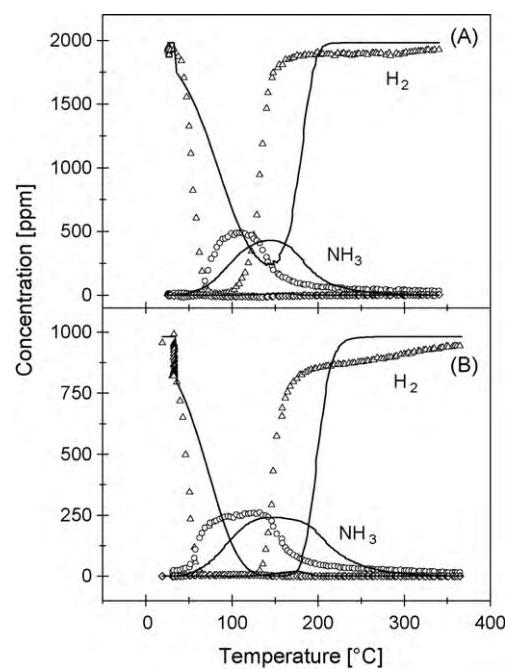
**Fig. 4.** Isothermal reduction with H<sub>2</sub> of NO<sub>x</sub> stored at 350 °C: (A) T = 150 °C; (B) T = 200 °C; (C) T = 250 °C; (D) T = 350 °C. Experimental effluent concentration of H<sub>2</sub>, NH<sub>3</sub> and N<sub>2</sub> at the MS detector, open symbols; model prediction of effluent concentration of H<sub>2</sub>, NH<sub>3</sub> and N<sub>2</sub> at the MS detector, full lines; model prediction of effluent concentration of NH<sub>3</sub> at the reactor exit, dashed lines. The inlet concentration of H<sub>2</sub> is set at 1000 ppm at t = 0.

give NH<sub>3</sub>) is faster than step S5 (reaction of nitrates with NH<sub>3</sub> to give N<sub>2</sub>). This is in line with the results in Fig. 1 showing only a very limited conversion of ammonia to nitrogen at the same temperature. Effluent NH<sub>3</sub> is detected with a large time delay due to NH<sub>3</sub> adsorption-desorption on the Mass Spec capillary. At 200 °C (panel B) immediately upon hydrogen admission the consumption of H<sub>2</sub> is complete, and only nitrogen is observed among the products. This is due to the fact that NH<sub>3</sub> produced through step S4 is consumed through step S5, which indeed at 200 °C is expectedly faster than at 150 °C. At higher regeneration times a decrease in the effluent nitrogen concentration is observed which again anticipates the increase in the concentration of effluent NH<sub>3</sub>, due to ammonia adsorption-desorption onto the Mass Spec capillary line. The increase in effluent NH<sub>3</sub> concentration is observed in correspondence to the hydrogen breakthrough due to the ammonia time delay. At higher temperatures (i.e. 250 °C in panel C and 350 °C in panel D) the amount of effluent ammonia detected during the experiment is much smaller because the relative importance of the rate of ammonia consumption (step S5) as compared to that of ammonia production (step S4) increases with temperature, i.e. the process is less kinetically controlled by step S5 as the temperature increases. At these high temperatures ammonia is detected well after the hydrogen breakthrough.

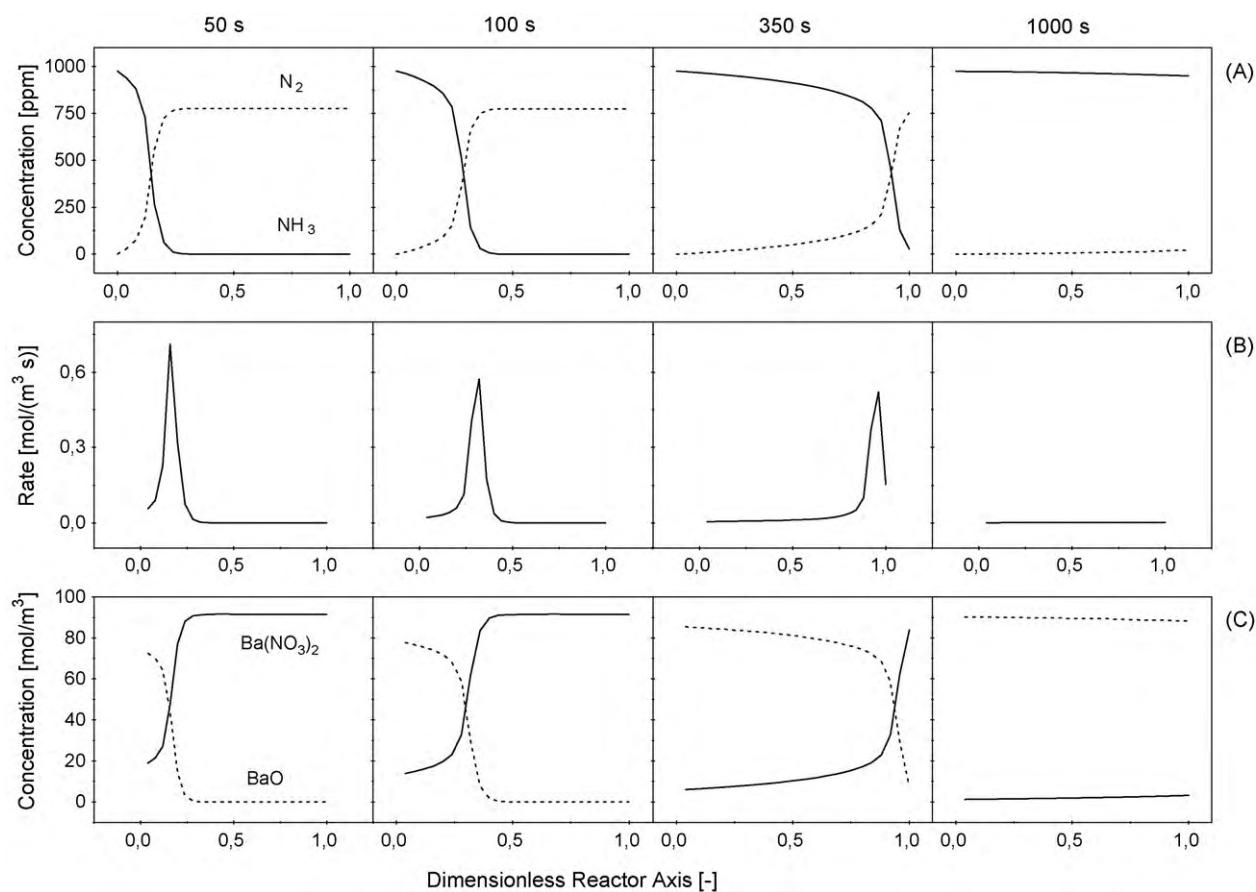
From these experiments and the final reduction run accomplished thereafter at 350 °C it is possible to calculate for each temperature the moles of NO<sub>x</sub> reduced by H<sub>2</sub> to form nitrogen (after the time period shown in Fig. 4 and till the end of the experiment) and also the sum of these moles with those that are reduced at 350 °C; these last ones correspond to those previously stored onto the catalyst at 350 °C. These quantities are listed in Table 4. In the same table the reduction efficiency at the end of the isothermal experiments, defined as the ratio between the moles of NO<sub>x</sub>

reduced at a given temperature to the sum of these moles with those that are reduced thereafter at 350 °C, is also given. The NO<sub>x</sub> reduction efficiency is close to 100% at any temperature. The comparison between the moles of NO<sub>x</sub> consumed during the reduction with H<sub>2</sub> and with NH<sub>3</sub> at low temperatures (150 and 200 °C) confirms that step S4 is faster than step S5.

The values of the parameter estimates obtained by regression of the experimental data in Fig. 4 are shown in Table 5. The model predictions (full lines) and the experimental effluent concentrations (open symbols) are compared in Fig. 4. The concentration profiles of both products NH<sub>3</sub> and N<sub>2</sub> and the breakthrough time of the reagent H<sub>2</sub> are well predicted by the model at any temperature. In Fig. 4 the reaction is limited by the concentration of the reducing agent up to a consumption of about 1.5–2 × 10<sup>-4</sup> mol NO<sub>x</sub>/g<sub>cat</sub>. Accordingly, on the basis of the previous analysis of regeneration of stored NO<sub>x</sub> with ammonia, the low activation energy estimated for the reduction of nitrates to NH<sub>3</sub> (22.94 kJ/mol) applies to residual NO<sub>x</sub> species far from the Pt crystallites and the reaction is limited by the surface mobility of the stored NO<sub>x</sub> species. Accordingly the use of the kinetic parameters for step S4 in Table 5 up to the consumption of about 1 × 10<sup>-4</sup> mol NO<sub>x</sub>/g<sub>cat</sub>, that on the basis of the present study are associated to more reactive Ba sites close to Pt crystallites, is expected to underestimate the true rate of regeneration by hydrogen. Again the delay of the effluent ammonia concentration can be appreciated by comparing the concentration of ammonia predicted by the model at the MS detector (full lines) and at the reactor exit (dashed lines). At 150 °C in panel A the ammonia concentration at the reactor exit is high immediately after hydrogen admission while at the MS detector is predicted by the model only after 40 s. The breakthrough of ammonia at the reactor exit predicted by the



**Fig. 5.** H<sub>2</sub>-TPSR runs performed with 1% H<sub>2</sub>O in the feed after NO<sub>x</sub> adsorption at 350 °C: (A) 2000 ppm of H<sub>2</sub>; (B) 1000 ppm of H<sub>2</sub>. Experimental effluent concentration of H<sub>2</sub>, NH<sub>3</sub> and N<sub>2</sub> at the MS detector, open symbols; model prediction of effluent concentrations of H<sub>2</sub>, NH<sub>3</sub> and N<sub>2</sub> at the MS detector, full lines.



**Fig. 6.** Gas phase concentration of NH<sub>3</sub> (full line) and N<sub>2</sub> (dashed line) [panel A], rate of reduction of Ba-nitrate to give nitrogen [panel B] and surface concentration of Ba(NO<sub>3</sub>)<sub>2</sub> (full line) and BaO (dashed line) [panel C] along the axial reactor coordinate at 300 °C at different regeneration times.

model (dashed lines) occurs before the H<sub>2</sub> breakthrough at 200 °C in panel B, together with the hydrogen breakthrough at 250 °C in panel C and after the hydrogen breakthrough at 350 °C in panel D. This behaviour originates from both the in series reaction scheme, where the reduction of nitrates by ammonia to give nitrogen follows the reduction of nitrates with hydrogen to give NH<sub>3</sub>, and the integral behaviour of the reactor, that will be addressed later.

A validation of the kinetic model of the reduction of stored NO<sub>x</sub> by H<sub>2</sub> was attempted by comparing experimental data collected during TPSR runs performed with 2000 and 1000 ppm of H<sub>2</sub> with 1% H<sub>2</sub>O in the feed with model predictions without any adjustment of the parameter estimates. The results shown in Fig. 5 demonstrate that the model is able to capture the onset temperature of the reduction process and the formation of only ammonia among the products, but underestimates the consumption of hydrogen and the net production of ammonia at low *T*, i.e. below 100 °C. This is because the kinetic parameters in Table 5 apply only above a consumption of 1.5–2 × 10<sup>-4</sup> mol NO<sub>x</sub>/g<sub>cat</sub> where the residual stored NO<sub>x</sub> are associated to less reactive Ba sites far from the Pt crystallites. Accordingly the model underestimates the true rate of regeneration of the more reactive Ba-nitrates close to the Pt crystallites that are reduced at first at low temperature.

### 3.3. Spatiotemporal resolution of LNT regeneration provided by the model

The model was used to simulate the axial concentration profiles in the reactor for gas and surface species as function of time during the reduction of stored NO<sub>x</sub> with ammonia at different temperatures.

The gas phase concentration of NH<sub>3</sub> and N<sub>2</sub>, the rate of reduction of Ba-nitrate to give nitrogen and the surface concentration of Ba(NO<sub>3</sub>)<sub>2</sub> and BaO along the axial coordinate of the reactor at 300 °C are plotted at different times in Fig. 6. It is worth noting that the model prediction in Fig. 6 do not consider the ammonia delay that occurs downstream of the reactor in the MS capillary. NH<sub>3</sub> is consumed completely within a given length of the front part of the reactor and reaches a zero concentration downstream (panel A). The region where ammonia is consumed results in the production of N<sub>2</sub> (panel A); the reaction is confined in this region and the rate of reaction is limited by the concentration of the reducing agent to the value of ca 0.5–0.6 mol/m<sub>cat</sub><sup>3</sup> s (panel B). The ammonia front moves towards the end of the reactor with time and the breakthrough is eventually observed at ca 350 s (dashed line in Fig. 1 panel D). N<sub>2</sub>, the end product of the reduction process, is detected immediately at the exit of the reactor; it reaches the maximum concentration of 800 ppm immediately/after few seconds (about 10 s) and starts to decrease after the ammonia breakthrough (350 s). NH<sub>3</sub> is consumed at the expense of Ba-nitrates (panel C); its surface concentration at first decreases sharply to a non-nil residual value in a confined region of the reactor. As time goes on the Ba(NO<sub>3</sub>)<sub>2</sub> consumption front moves towards the exit of the reactor, that is eventually reached at 350 s. In the meantime the residual surface concentration of Ba(NO<sub>3</sub>)<sub>2</sub> left behind the consumption front decreases slowly and progressively: at the entrance of the reaction it decreases from 20 mol/m<sub>cat</sub><sup>3</sup> at 50 s down to 6 mol/m<sub>cat</sub><sup>3</sup> at 350 s and to 1.3 mol/m<sub>cat</sub><sup>3</sup> at 1000 s. On the opposite the surface concentration of BaO increases in a parallel way because during reduction Ba-nitrates are transformed into BaO. As already noted BaO can be likely transformed into Ba(OH)<sub>2</sub> due to the presence of large amounts of water in the gas phase. The peculiar features of the Ba(NO<sub>3</sub>)<sub>2</sub> consumption and of its dynamics as the regeneration proceeds is due to the presence of fast and slow regeneration sites that are described in the model by a coverage dependent energy of activation for step S5. The Ba-nitrates close to the metal crystallites react first and are responsible for the development of the Ba(NO<sub>3</sub>)<sub>2</sub>

consumption front while the Ba-nitrates far from the metal crystallites are left behind the consumption front and are consumed later on. Since the catalyst has been saturated during the previous storage phase both fast and slow storage/regeneration sites have been occupied at any axial position of the LNT reactor during storage and the amount of the fast sites according to the present kinetic study corresponds roughly to the value of 4 × 10<sup>-3</sup> mol Ba(NO<sub>3</sub>)<sub>2</sub>/m<sub>cat</sub><sup>3</sup>, i.e. 1 × 10<sup>-4</sup> mol NO<sub>x</sub>/g<sub>cat</sub>.

At lower temperature (not shown) the rate of reaction is lower and the region where ammonia is consumed is larger. Also the ammonia breakthrough and the concomitant decline in the concentration of effluent nitrogen are observed earlier, namely at 300 s for *T*=250 °C and at 10 s for *T*=200 °C (see Fig. 1 panels C and B, respectively). At 250 °C a surface concentration front of Ba(NO<sub>3</sub>)<sub>2</sub>, that travels with time along the reactor axis, is still predicted by the model but is more smooth and the change with time of the residual concentration of Ba(NO<sub>3</sub>)<sub>2</sub> left behind the concentration front is slower. At 200 °C the reaction rate is lower and the reaction is no longer confined in a portion of the reactor where it is limited by the concentration of the reducing agent. Accordingly a spatially confined concentration front of Ba(NO<sub>3</sub>)<sub>2</sub> is no longer apparent and the axial profile of the concentration of Ba(NO<sub>3</sub>)<sub>2</sub> develops along the entire length of the reactor. At 150 °C the axial profile of the gas and surface species are almost flat and a significant concentration of Ba(NO<sub>3</sub>)<sub>2</sub> is still present after prolonged reaction time due to the very low rate of reaction.

The same spatiotemporal analysis was not attempted for the regeneration of stored NO<sub>x</sub> with hydrogen, because the kinetic parameters estimated for step S4 in the present study are valid only after a consumption of 1.5–2 × 10<sup>-4</sup> mol NO<sub>x</sub>/g<sub>cat</sub> and the model underestimates the reactivity of fast regeneration sites.

## 4. Conclusions

A kinetic model based exclusively on a consecutive reaction scheme with ammonia as intermediate was developed which includes adsorption-desorption of hydrogen, ammonia and water at Pt site, the reduction of stored nitrates by hydrogen to give ammonia and the reduction of stored nitrates by ammonia to give nitrogen. The delay in the ammonia signal observed in the experiments was described by NH<sub>3</sub> adsorption-desorption occurring onto the Mass Spec capillary line in series to the catalytic reactor. The model was shown to capture the major features of the isothermal experiments performed over a Pt-BaO/Al<sub>2</sub>O<sub>3</sub> catalyst with hydrogen and ammonia as reducing agents in the *T* interval 150–350 °C and under wet conditions.

The rate constants of adsorption-desorption of hydrogen, ammonia and water were taken from the literature (except the pre-exponential factor of ammonia desorption) while the other parameters were estimated by regression to the experiments. A surface dependent energy of activation was assumed for the reduction of stored nitrates by ammonia to give nitrogen in order to describe the data collected in the investigated temperature interval when ammonia was employed as the reducing agent. This is explained with the presence of nitrates with high and low reactivity that are envisaged as close or far from the noble metal crystallites, respectively. Besides a low energy of activation was estimated for the reduction of nitrates by hydrogen to give ammonia. This view applies for a consumption level of stored NO<sub>x</sub> above 1.5–2 × 10<sup>-4</sup> mol NO<sub>x</sub>/g<sub>cat</sub>, where the NO<sub>x</sub> species are expectedly stored far from the Pt crystallites, and the reaction is limited by surface diffusion. Below this consumption value the reaction is limited by the concentration of the reducing agent at any temperature.

The model was validated against independent NH<sub>3</sub>- and H<sub>2</sub>-TPSR data. A very nice agreement was obtained for the NH<sub>3</sub>-TPSR

data but the model underestimated the consumption of hydrogen at high concentration of Ba-nitrates and at low temperature during H<sub>2</sub>-TPSR. This is because the kinetic model underestimates the true rate of regeneration with hydrogen of the most reactive Ba-nitrates close to the Pt crystallites, that are reduced at first at low temperature.

The model was also used to simulate the axial concentration profiles in the reactor for gas and surface species as function of time during the regeneration of the LNT catalyst with ammonia. During regeneration an ammonia front develops which moves towards the end of the reactor and eventually breaks through while nitrogen, the end product of the reduction process, is detected immediately at the exit of the reactor, reaches the maximum concentration of 800 ppm after few seconds and decreases only after the ammonia breakthrough. Also a consumption front of Ba-nitrates develops which travels towards the end of the reactor and eventually it breaks through. The consumption front is associated with most reactive Ba-nitrates in close proximity to the Pt crystallites. In the same time a residual concentration of Ba(NO<sub>3</sub>)<sub>2</sub>, associated with less reactive nitrates stored far from the Pt crystallites, is left behind the consumption front, which decreases slowly and progressively with time.

The kinetic model developed in the present paper differs from those available in the literature because it considers the most relevant physico-chemical features of regeneration of LNT catalysts under nearly isothermal conditions. These include a mechanism based only on surface reaction of stored NO<sub>x</sub>, a pathway consisting exclusively of a consecutive reaction scheme with ammonia as intermediate and the presence of slow and fast reduction sites associated with NO<sub>x</sub> stored close and far from the noble metal crystallites, respectively.

## References

- [1] L. Lietti, I. Nova, P. Forzatti, *Catal. J.* 257 (2008) 270–282.
- [2] N. Takahashi, H. Shinjoh, T. Iijima, T. Suzuki, K. Yamazaki, K. Yokota, H. Suzuki, N. Miyoshi, S. Matsumoto, T. Tanizawa, T. Tanaka, S. Tateishi, K. Kasahara, *Catal. Today* 27 (1996) 63–69.
- [3] W.S. Epling, L.E. Campbell, A. Yezersets, N.W. Currier, J.E. Parks, *Catal. Rev.: Sci. Eng.* 46 (2004) 163–245.
- [4] L. Lesage, C. Verrier, P. Bazin, J. Saussey, M. Daturi, *Phys. Chem. Chem. Phys.* 5 (2003) 4435–4440.
- [5] L. Lesage, C. Verrier, P. Bazin, J. Saussey, S. Malo, C. Hedouin, G. Blanchard, M. Daturi, *Top. Catal.* 30–31 (2004) 31–36.
- [6] L. Castoldi, I. Nova, L. Lietti, P. Forzatti, *Catal. Today* 96 (2004) 43–52.
- [7] J. Parks, S. Huff, J. Phil, J.-S. Choi, B. West, SAE Technical Paper 2005-01-3876, 2005.
- [8] J.A. Pihl, J.E. Parks, C.S. Daw, T.W. Root, SAE Technical Paper 2006-01-3441, 2006.
- [9] I. Nova, L. Castoldi, L. Lietti, E. Tronconi, P. Forzatti, *Top. Catal.* 42–43 (2007) 21–25.
- [10] I. Cumaranatunge, S.S. Mulla, A. Yezersets, N.W. Currier, W.N. Delgass, F.H. Ribeiro, *J. Catal.* 246 (2007) 29–34.
- [11] S.S. Mulla, S.S. Chaugule, A. Yezersets, N.W. Currier, W.N. Delgass, F.H. Ribeiro, *Catal. Today* 136 (2008) 136–145.
- [12] J.-S. Choi, W.P. Partridge, J.A. Pihl, C.S. Daw, *Catal. Today* 136 (2008) 173–182.
- [13] I. Nova, L. Lietti, P. Forzatti, *Catal. Today* 136 (2008) 128–135.
- [14] P. Forzatti, L. Lietti, I. Nova, *Energy Environ. Sci.* 1 (2008) 236–247.
- [15] R.D. Clayton, M.P. Harold, V. Balakotaiah, *Appl. Catal. B* 84 (2008) 616–630.
- [16] W.P. Partridge, J.-S. Choi, *Appl. Catal. B* 91 (2009) 144–151.
- [17] I. Nova, L. Lietti, L. Castoldi, E. Tronconi, P. Forzatti, *J. Catal.* 239 (2006) 244.
- [18] P. Forzatti, L. Lietti, *Catal. Today* (2009), doi:10.1016/j.cattod.2008.11.023.
- [19] H. Mazhoul, J.F. Brilhac, P. Gilot, *Appl. Catal. B* 20 (1999) 47–55.
- [20] L. Olsson, H. Persson, E. Fridel, M. Skoglundh, B. Andersson, *J. Phys. Chem. B* 105 (2001) 196–209.
- [21] L. Olsson, E. Fridel, M. Skoglundh, B. Andersson, *Catal. Today* 73 (2002) 263–270.
- [22] A. Lindhom, N.W. Currier, J. Li, A. Yezersets, L. Olsson, *J. Catal.* 258 (2008) 273–288.
- [23] J. Xu, R. Clayton, V. Balakotaiah, M. Harold, *Appl. Catal. B* 77 (2008) 395–408.
- [24] R.S. Larson, J.A. Pihl, V.K. Chakravarthy, T.J. Toops, C.S. Daw, *Catal. Today* 136 (2008) 104–120.
- [25] A. Guthenke, D. Chatterjee, M. Weibel, N. Waldbußer, P. Koci, M. Marek, M. Kubicek, *Chem. Eng. Sci.* 62 (2007) 5357–5363.
- [26] P. Koci, F. Plat, J. Stepanek, M. Kubicek, L. Marek, *Catal. Today* 137 (2008) 253–260.
- [27] U. Tuttles, V. Schmeisser, G. Eigenberger, *Chem. Eng. Sci.* 59 (2004) 4731–4738.
- [28] L. Olsson, R.J. Blint, E. Fridell, *Ind. Eng. Chem. Res.* 44 (2005) 3021–3032.
- [29] L. Olsson, D. Monroe, R. Blint, *Ind. Eng. Chem. Res.* 45 (2006) 8883–8890.
- [30] M. Sharma, R. Clayton, M.P. Harold, V. Balakotaiah, *Chem. Eng. Sci.* 62 (2007) 5176–5181.
- [31] M. Sharma, M.P. Harold, V. Balakotaiah, *Ind. Eng. Chem. Res.* 44 (2005) 6264–6277.
- [32] C.M.L. Scholtz, V.R. Gangwal, M. de Croon, J.C. Shoultten, *J. Catal.* 245 (2007) 215–227.
- [33] L. Cao, J.L. Ratts, A. Yezersets, N.W. Currier, J.M. Caruthers, F.H. Ribeiro, N.W. Delgass, *Ind. Eng. Chem. Res.* 47 (2008) 9006–9017.
- [34] D. Bhatia, R.D. Clayton, M.P. Harold, V. Balakotaiah, *Catal. Today* 147S (2009) S250–S256.
- [35] M. Boudard, G. Djéga-Mariadassou, *Kinetics of Heterogeneous Catalytic Reactions*, Princeton University Press, Princeton, NJ, 1984.
- [36] F. Frola, M. Manzoli, F. Prinetto, G. Ghiootti, L. Castoldi, L. Lietti, *J. Phys. Chem. C* 112 (2008) 12869–12878.
- [37] I. Nova, L. Castoldi, L. Lietti, E. Tronconi, P. Forzatti, F. Prinetto, G. Ghiootti, *J. Catal.* 222 (2004) 377–388.
- [38] R. Rinnemo, O. Deutschmann, F. Behrendt, B. Kasemo, *Comb. Flame* 111 (4) (1997) 312–326.
- [39] J.J. Vajo, W. Tsai, W.H. Weinberg, *J. Phys. Chem.* 89 (15) (1985) 3243–3251.
- [40] G. Buzzi-Ferraris, F. Manenti, *Interpolation and Regression Models for the Chemical Engineer Solving Numerical Problems*, Wiley-VCH, Weinheim, Germany, 2009, ISBN: 978-3-527-32651-5.
- [41] G. Buzzi-Ferraris, F. Manenti, *Chem. Eng. Sci.* 64 (2009) 1061–1074.
- [42] G. Zhou, L.T. Lou, R.J. Gorte, *Appl. Catal. B* 64 (2006) 88–95.
- [43] N.W. Cant, I.O.Y. Liu, M.J. Patterson, *Catal. J.* 243 (2006) 309–317.
- [44] I. Nova, L. Castoldi, F. Prinetto, V. Dal Santo, L. Lietti, E. Tronconi, P. Forzatti, G. Ghiootti, R. Psaro, S. Recchia, *Top. Catal.* 52 (2009) 1757–1761.